## Analysis and Design of Analog Integrated Circuits Lecture 4

Small Signal Modeling of CMOS Transistors

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## Lecture 3 Discussed Large Signal Calculations

- In analog circuits, we are often focused on amplifiers in which the small signal behavior is of high importance
  - Large signal calculations lead to the operating point information of the circuit which is used to determine the small signal model of the device
- Example amplifier circuit:





## A Key Design Parameter is the Sizing of Devices



- The designer is generally free to choose the width (W) and length (L) of the device
  - Wider width is often chosen to achieve higher channel current for a given gate bias voltage
  - Longer length is often avoided since it lowers the channel current and decreases the operating speed of the device
    - The minimum length for the gate is often used to define the process name (i.e., 0.18u CMOS or 0.13u CMOS)
    - Longer length is used in cases where better matching or high resistance is desired

#### MOS DC Small Signal Model (Saturation Assumed)



#### How do we model if device is in the triode region?

### **CMOS Devices Also Have Capacitance**



channel to bulk cap: C<sub>cb</sub> - ignore in this class *M.H. Perrott* 

#### MOS AC Small Signal Model (Device in Saturation)



$$\begin{split} C_{gs} &= C_{gc} + C_{ov} = \frac{2}{3} C_{ox} W(L-2L_D) + C_{ov} \\ C_{gd} &= C_{ov} \\ C_{sb} &= C_{jsb} \quad (\text{area + perimeter junction capacitance}) \\ C_{db} &= C_{jdb} \quad (\text{area + perimeter junction capacitance}) \end{split}$$

### Small Signal Modeling Strategy

- We will focus on the DC Small Signal Model first
  - This will allow us to calculate the gain of amplifiers
  - This will also allow us to derive Thevenin resistances
    - We will later combine this information with the capacitors within the AC Small Signal Model to estimate frequency response information
- Homework 1 should have revealed to you how clumsy the DC Small Signal Model can be in calculations
  - We need a more streamlined approach
    - Strategy: give up general approach, and focus on achieving a simpler model that fits a large number of circuit topologies that we will encounter

# **Thevenin Modeling of CMOS Transistors**



We will discuss weak inversion (i.e., subthreshold region) later

- Use the Hybrid-π model of transistor to calculate Thevenin resistances at each transistor node
- Use these Thevenin resistance calculations for many circuit topologies that we encounter

## Thevenin Resistance Expressions



### Replace Hybrid- $\pi$ Model with Proposed Thevenin Model



## Key Things to Know About the Proposed Thevenin Model



- This model may be generally applied in cases where the transistor is in saturation and where there is not strong interaction between the transistor terminals
  - Works well for open loop amplifier stages which will be our initial focus
- Proposed model is not commonly taught I developed it

## A General View of Signal Flow in an Open Loop Device



To first order, influence of signals go from gate to source or from gate and/or source to drain

This is only true when the device is in saturation

## **Example:** Small Signal Analysis of Amplifier Circuit



Key device characteristics that must be known:

For  $\mathbf{g}_{m}$ ,  $\mathbf{r}_{o}$ : W, L,  $\mu_{n}\mathbf{C}_{ox}$ ,  $\lambda$ 

For  $\mathbf{g}_{mb}$ :  $\mathbf{g}_{m}$ ,  $\gamma$ ,  $\Phi_{F}$ ,  $V_{SB}$ 

- First step: determine the operating region of transistor
  - For triode region, approximate channel as a resistance
    - I<sub>d</sub> will usually be set primarily by drain and source network
  - For subthreshold region, approximate channel as open
    - Later on, we will take a more accurate view of this
  - For saturation region, use proposed Thevenin model
    - I<sub>d</sub> will usually be set by gate voltage and source network (i.e., resistance and voltage)
    - Small signal parameters (g<sub>m</sub>, r<sub>o</sub>, etc.) can be calculated once I<sub>d</sub> is known

## Substitute Proposed Thevenin Model (Assumes Saturation)



Notice that all voltages and currents can be calculated without requiring simultaneous equations!

#### **Reduce to Two-Port**



Calculation of G<sub>m</sub>:

$$\alpha i_s = i_s = \frac{A_v}{R_{th_s} + R_s} v_g \approx \frac{1}{1/g_m + R_s} v_g = \frac{g_m}{1 + g_m R_s} v_g = G_m v_g$$

## **Detailed Example**



Assumptions:

- Determine operating point conditions
  - Transistor operating region, I<sub>d</sub>
- Determine small signal parameters of transistor model
  - If transistor is in saturation, this is g<sub>m</sub>, r<sub>o</sub>, etc.
- Determine gain of amplifier